

# Quantum Cryptography with Local Bell Tests

<u>Charles Ci Wen Lim</u>, Christopher Portmann, Marco Tomamichel, Renato Renner and Nicolas Gisin

A project between University of Geneva and ETH Zurich







### Inception

Bennett and Brassard 1984



I. Prepare single photons in the computational or diagonal basis





## Inception

Bennett and Brassard 1984





2. Measures them in the computational or diagonal basis

Experiment done in QCRYPT Conference Dinner 2011

 arXiv.org > quant-ph > arXiv:quant-ph/0212066
 Search

 Quantum Physics

 Security of quantum key distribution with imperfect devices

 Daniel Gottesman, Hoi-Kwong Lo, Norbert Lütkenhaus, John Preskill

 (Submitted on 11 Dec 2002 (v1), last revised 3 Sep 2004 (this version, v3))

 We prove the security of the Bennett-Brassard (BB84) quantum key distribution protocol in the case where the source and detector are under the limited control of an adversary. Our proof applies when both the source and the detector have small basis-dependent flaws, as is typical in practical implementations of the protocol. We derive a general lower bound on the asymptotic key generation rate for weakly basis-dependent eavesdropping attacks, and also estimate the rate in some special cases: sources that emit weak coherent states with random phases, detectors with basis-dependent efficiency, and misaligned sources and detectors.



ar)	rXiv.org > quant-ph > arXiv:quant-ph/0212066											
Qı	arXi	rXiv.org > quant-ph > arXiv:quant-ph/0411004										
S	Qu	arXiv.org > quant-ph > arXiv:0708.0709										
Da (Su	De	Quantum Physics										
	Hoi <i>(Sut</i>	Quantum cryptography with finite resources: unconditional security bound for discrete-variable protocols with one-way post-processing										
	i	Valerio Scarani, Renato Renner										
	-	(Submitted on 6 Aug 2007 (v1), last revised 1 Jun 2008 (this version, v2))										
	e f I	We derive a bound for the security of QKD with finite resources under one-way post-processing, based on a definition of security that is composable and has an operational meaning. While our proof relies on the assumption of collective attacks, unconditional security follows immediately for standard protocols like Bennett-Brassard 1984 and six-states. For single-qubit implementations of such protocols, we find that the secret key rate becomes positive when at least N\sim 10^5 signals are exchanged and processed. For any other discrete-variable protocol, unconditional security can be obtained using the exponential de Finetti theorem, but the additional overhead leads to very pessimistic estimates.										





arXiv.org > quant-ph > arXiv:quant-ph/0212066											
QIar	arXiv.org > quant-ph > arXiv:quant-ph/0411004										
SI QI	Qu arXiv.org > quant-ph > arXiv:0708.0709										
Da D	•	Qu	arXi	rXiv.org > quant-ph > arXiv:0804.3082							
Ho (Su	<sup>,</sup> (	Q bi	Qua	arXiv	iv.org > quant-ph > arXiv:1011.2982						
		Va	Sq	Qua	arXiv.org > quant-ph > arXiv:1103.4130	ation					
	6	(Su	Nori (Subi	Us	Quantum Physics						
	e f I		M	<mark>Chi-</mark> (Subr	Tight Finite-Key Analysis for Quantum Cryptography	ral on of a					
_	1		m a	Tł in pr	Marco Tomamichel, Charles Ci Wen Lim, Nicolas Gisin, Renato Renner (Submitted on 21 Mar 2011)	present					
			sc st fc	ac m in re m th sc th cc to th pr te	Despite enormous progress both in theoretical and experimental quantum cryptography, the security of most current implementations of quantum key distribution is still not established rigorously. One of the main problems is that the security of the final key is highly dependent on the number, M, of signals exchanged between the legitimate parties. While, in any practical implementation, M is limited by the available resources, existing security proofs are often only valid asymptotically for unrealistically large values of M. Here, we demonstrate that this gap between theory and practice can be overcome using a recently developed proof technique based on the uncertainty relation for smooth entropies. Specifically, we consider a family of Bennett–Brassard 1984 quantum key distribution protocols and show that security against general attacks can be guaranteed already for moderate values of M.	the six- Iropper					

arXiv.org > quant-ph > arXiv:quant-ph/0212066													
QI ar)	(iv.or	.org > quant-ph > arXiv:quant-ph/0411004											
SI Qu	ar)	rXiv.org > quant-ph > arXiv:0708.0709											
Da Da	Qu	arXiv.org > quant-ph > arXiv:0804.3082											
Ho (Su	<sup>t</sup> D	Qua	arXiv.org > quant-ph > arXiv:1011.2982										
	1 1 Va	Sq	Qua 11n	arXi	v.org > quant-ph > arXiv:1103.4130	tion							
	r (Su. r	(Subi	Us	Qua	arXiv.org > quant-ph > arXiv:1107.0589								
	f	м	Chi- (Subr	Τi	Quantum Physics								
-		m a	Tł in pr	Mar (Sub	Concise and Tight Security Analysis of the Bennett-Brassard 1984 Protocol with Finite Key Lengths	of a esent							
	-	st	ac m in	D	Masahito Hayashi, Toyohiro Tsurumaru	oper							
		fo	re m	n	(Submitted on 4 Jul 2011 (v1), last revised 17 May 2012 (this version, v2))								
			th sc to to th pr te the	e: a' Vi re Ci a eorem.	We present a tight security analysis of the Bennett-Brassard 1984 protocol taking into account the finite size effect of key distillation, and achieving unconditional security. We begin by presenting a concise analysis utilizing the normal approximation of the hypergeometric function. Then next we show that a similarly tight bound can also be obtained by a rigorous argument without relying on any approximation. In particular, for the convenience of experimentalists who wish to evaluate the security of their QKD systems, we also give explicit procedures of our key distillation, and also show how to calculate the secret key rate and the security parameter from a given set of experimental parameters. Besides the exact values of key rates and security parameters, we also present how to obtain their rough estimates using the normal approximation.								

arXiv.org > quant-ph > arXiv:quant-ph/0212066											
Q	arXi	iv.or	org > quant-ph > arXiv:quant-ph/0411004								
S	Qu	arX	Xiv.org > quant-ph > arXiv:0708.0709								
Da (SL	De Hoi (Sut	Qu	arXi	arXiv.org > quant-ph > arXiv:0804.3082							
		Q	Qua	arXiv	/.org >	> quar	Nt-ph > arXiv:1011.2982				
	1	Va (Su	Sq	Qua	arXi	iv.org	y > quant-ph > arXiv:1103.4130				
	r r e		Nori (Subi	Us	Qua	arXi	v.org > quant-ph > arXiv:1107.0589				
	f		м	Chi- (Subr	Τi	Qua	arXiv.org > quant-ph > arXiv:1109.1473				
1	-		m m	Tł	Mar	Co	Quantum Physics				
	l		a sc	pr ac	(Sub	19	Measurement-device-independent quantum key distribution				
			st fo	in re	n	Mas (Sub	Hoi-Kwong Lo, Marcos Curty, Bing Qi				
		. 1	-	m	n e:	(Sub	(Submitted on 7 Sep 2011 (v1), last revised 28 May 2012 (this version, v2))				
				sc th cc to th pr te the	a Vi re Ci a eorem.	e u b ti e s s	How to remove detector side channel attacks has been a notoriously hard problem in quantum cryptography. Here, we propose a simple solution to this problem*measurement* device independent quantum key distribution. It not only removes all detector side channels, but also doubles the secure distance with conventional lasers. Our proposal can be implemented with standard optical components with low detection efficiency and highly lossy channels. In contrast to the previous solution of full device independent QKD, the realization of our idea does not require detectors of near unity detection efficiency in combination with a qubit amplifier (based on teleportation) or a quantum non-demolition measurement of the number of photons in a pulse. Furthermore, its key generation rate is many orders of magnitude higher than that based on full device independent QKD. The results show that long-distance quantum cryptography over say 200km will remain secure even with seriously flawed detectors.				

arX	rXiv.org > quant-ph > arXiv:quant-ph/0212066											
Qı	arXi	Search o Search o Search o										
S	Qu	arXiv.org > quant-ph > arXiv:0708.0709										
Da (Sı	De Hoi (Sut	Qu	arXi	arXiv.org > quant-ph > arXiv:0804.3082								
		Q bu Va	Qua Sq	arXiv	Xiv.org > quant-ph > arXiv:1011.2982							
				Qua	arXi	iv.or	g >	quant-ph > arXiv:1103.4130				
	r r	(Su	Nori (Subi	Us	Qua	arX	iv.o	rg > quant-ph > arXiv:1107.0589				
1	f		M	Chi- (Subr	Ti	Qua	ar)	Kiv.org > quant-ph > arXiv:1109.1473				
	-		m	Tł in	Mar (Sub	Cc 19	Qu	arXiv.org > quant-ph > arXiv:1109.2330				
	.,	-	sc st	ac m	D	Mas	Μ	Quantum Physics				
		۰,	fc	in re m	n n	(Sub	Ho (Su	Side-channel-free quantum key distribution				
				th sc th	e: av	V e		Samuel L. Braunstein, Stefano Pirandola				
				cc	vi re	u b		(Submitted on 11 Sep 2011 (v1), last revised 6 Jun 2012 (this version, v2))				
				th pr	C	t		Quantum key distribution (QKD) offers the promise of absolutely secure communications. However, proofs of absolute security often assume perfect implementation from theory to experiment. Thus, existing				
				te the	eorem.	S		systems may be prone to insidious side-channel attacks that rely on flaws in experimental implementation.				
				_	_	5		settings inside private spaces inaccessible while simultaneously acting as a Hilbert space filter to eliminate				
								side-channel attacks. By using a quantum memory we find that we are able to bound the secret-key rate below by the entanglement-distillation rate computed over the distributed states.				













# Imperfect devices

In reality, most practical devices do not conform to the required theoretical models.

![](_page_21_Picture_2.jpeg)

# Imperfect devices

In reality, most practical devices do not conform to the required theoretical models.

However, if we know where an imperfect is, then we can measure it and include it in the security proof.

Examples: Basis mis-alignment, basis leakage, etc.

![](_page_22_Picture_4.jpeg)

# Imperfect devices

In reality, most practical devices do not conform to the required theoretical models.

However, if we know where an imperfect is, then we can measure it and include it in the security proof.

Examples: Basis mis-alignment, basis leakage, etc.

In the case of basis leakage, we have to give this additional information to the adversary,

![](_page_23_Picture_5.jpeg)

$$K_{\text{rate}} = 1 - h_2(e_{\text{phase}}) - h_2(e_{\text{bit}})$$
$$e_{\text{phase}} \le e_{\text{X}} + 4\Gamma + 4\sqrt{\Gamma e_{\text{X}}}$$

where  $\Gamma$  parameterizes the basis leakage.

For more details, refer to the works of Lo and Preskill (2007) and Gottesman et al (2004).

![](_page_25_Picture_1.jpeg)

Secure Lab

![](_page_26_Picture_1.jpeg)

![](_page_27_Figure_1.jpeg)

![](_page_28_Picture_1.jpeg)

![](_page_28_Picture_2.jpeg)

Basically, these are the channels which are not considered in the protocol tests.

# Asymptotic Limit

Pre-existing security proofs are obtained under the assumption that Alice and Bob exchange an infinite number of signals. Then, it is possible to obtain the secret key rate, e.g., for the BB84 protocol

$$K_{\text{rate}} = 1 - h_2(e_{\text{phase}}) - h_2(e_{\text{bit}})$$

![](_page_29_Picture_3.jpeg)

# Asymptotic Limit

Pre-existing security proofs are obtained under the assumption that Alice and Bob exchange an infinite number of signals. Then, it is possible to obtain the secret key rate, e.g., for the BB84 protocol

![](_page_30_Picture_2.jpeg)

$$K_{\text{rate}} = 1 - h_2(e_{\text{phase}}) - h_2(e_{\text{bit}})$$

To correct for the finite key size, **the basic idea is to give all the statistic fluctuations to the adversary**, i.e.,

$$\hat{K}_{\text{rate}} \approx 1 - h_2(e_{\text{phase}} + \Delta e_{\text{phase}}) - h_2(e_{\text{bit}} + \Delta e_{\text{bit}})$$

# Asymptotic Limit

Pre-existing security proofs are obtained under the assumption that Alice and Bob exchange an infinite number of signals. Then, it is possible to obtain the secret key rate, e.g., for the BB84 protocol

![](_page_31_Picture_2.jpeg)

$$K_{\text{rate}} = 1 - h_2(e_{\text{phase}}) - h_2(e_{\text{bit}})$$

To correct for the finite key size, **the basic idea is to give all the statistic fluctuations to the adversary**, i.e.,

$$\hat{K}_{\text{rate}} \approx 1 - h_2(e_{\text{phase}} + \Delta e_{\text{phase}}) - h_2(e_{\text{bit}} + \Delta e_{\text{bit}})$$

However, most of the finite-key security proofs assume that the devices are perfect.

![](_page_33_Picture_1.jpeg)

![](_page_33_Picture_2.jpeg)

Hidden Side-Channels

Devices are **imperfect** w.r.t the theoretical models used in the proof.

![](_page_34_Picture_1.jpeg)

a complete characterization of the devices

![](_page_35_Picture_1.jpeg)


Put all the parameters into the security proof

### What happens next?

Step 3: Add in all the statistical fluctuations



Most pre-existing proofs are valid only in the **asymptotic limit** 





Hidden Side-Channels

Devices are **imperfect** w.r.t the theoretical models used in the proof.



a complete characterization of the devices

• Step 2: Put all the parameters into the security proof

Although it appears possible to attain such a security proof, one can imagine....

Although it appears possible to attain such a security proof, one can imagine....

#### Disadvantages:

- Very likely to require a large amount of signals
- Cumbersome
- Requires more local randomness for parameter estimation phase
- Difficult to identify the entire set of discrepancies

Although it appears possible to attain such a security proof, one can imagine....

#### Disadvantages:

- Very likely to require a large amount of signals
- Cumbersome
- Requires more local randomness for parameter estimation phase
- Difficult to identify the entire set of discrepancies



An iceberg in QKD

Although it appears possible to attain such a security proof, one can imagine....

#### Disadvantages:

- Very likely to require a large amount of signals
- Cumbersome
- Requires more local randomness for parameter estimation phase
- Difficult to identify the entire set of discrepancies





#### An iceberg in $\mathsf{QKD}$

First, tackle the Trojan-horse attacks via the idea of Time-reversed EPR scheme

Biham, Huttner and Mor (1996) and Inamori (2005)

First, tackle the Trojan-horse attacks via the idea of Time-reversed EPR scheme

Biham, Huttner and Mor (1996) and Inamori (2005)



First, tackle the Trojan-horse attacks via the idea of Time-reversed EPR scheme

Biham, Huttner and Mor (1996) and Inamori (2005)





### Building a clean approach In this picture, one does not have the responsibility of the detectors. But Alice and Bob are still using ideal devices. Lo, Curty and Qi (2012) and Braunstein and Pirandola (2012)



Qn: It is too cumbersome to obtain a complete knowledge of all my local devices, I just want to use my devices, regardless of all those small discrepancies. Can I still generate secure keys with them?



Qn: It is too cumbersome to obtain a complete knowledge of all my local devices, I just want to use my devices, regardless of all those small discrepancies. Can I still generate secure keys with them?

Ans: The first yes: output a key (of zero length) and you get an unconditionally secure key. The second yes...



Qn: It is too cumbersome to obtain a complete knowledge of all my local devices, I just want to use my devices, regardless of all those small discrepancies. Can I still generate secure keys with them?

Ans: The first yes: output a key (of zero length) and you get an unconditionally secure key. The second yes...





and Lim et al (2012)



#### **Certification of BB84 states (limiting case)**

If the maximal violation of the CHSH test is observed, then the output states are the BB84 states.









#### **Advantages**

• Trojan-Horse and Blinding attacks free.



#### **Advantages**

- Trojan-Horse and Blinding attacks free.
- The devices only need to be characterized by one parameter, regardless of the number of discrepancies.





#### **Advantages**

- Trojan-Horse and Blinding attacks free.
- The devices only need to be characterized by one parameter, regardless of the number of discrepancies.
- The security proof is valid in the finite key size regime.





#### **Advantages**

- Trojan-Horse and Blinding attacks free.
- The devices only need to be characterized by one parameter, regardless of the number of discrepancies.
- The security proof is valid in the finite key size regime.



#### **Disadvantages**



#### **Advantages**

- Trojan-Horse and Blinding attacks free.
- The devices only need to be characterized by one parameter, regardless of the number of discrepancies.
- The security proof is valid in the finite key size regime.



#### **Disadvantages**

• Requires local entanglement sources.

$$K_{\infty} = 1 - 2h_2(e) - \log_2\left(1 + \frac{S}{4}\sqrt{8 - S^2}\right)$$

$$K_{\infty} = 1 - 2h_2(e) - \log_2\left(1 + \frac{S}{4}\sqrt{8 - S^2}\right)$$

Secret key fraction of the BB84 protocol

$$K_{\infty} = 1 - 2h_2(e) - \log_2\left(1 + \frac{S}{4}\sqrt{8 - S^2}\right)$$

Secret key fraction of the BB84 protocol Correction due to the imperfect devices

$$K_{\infty} = 1 - 2h_2(e) - \log_2\left(1 + \frac{S}{4}\sqrt{8 - S^2}\right)$$

Secret key fraction of the BB84 protocol Correction due to the imperfect devices





Pironio et al (2009), Mckague (2009), Hanggi and Renner (2010), Masanes, Pironio and Acin (2011).



Pironio et al (2009), Mckague (2009), Hanggi and Renner (2010), Masanes, Pironio and Acin (2011).

The Bell test is used to evaluate the quantum channel and devices!!

**Device-Independent QKD** achieves the same advantage but is limited directly by the channel loss, i.e., detection loophole

**Device-Independent QKD** achieves the same advantage but is limited directly by the channel loss, i.e., detection loophole

With **local Bell tests**, we do not have such a problem, in fact, we only need to consider local losses.

**Device-Independent QKD** achieves the same advantage but is limited directly by the channel loss, i.e., detection loophole

Can be rectified with Heralded Qubit Amplifier or Entanglement Swapping (See Gisin, Pironio, Sangouard (2010) and Curty and Moroder (2011)). With **local Bell tests**, we do not have such a problem, in fact, we only need to consider local losses.



The quantum channel - Bell Test Imperfect devices - Bell Test With **local Bell tests**, we do not have such a problem, in fact, we only need to consider local losses.


### **Related Work and Connections**



QKD with local Bell tests

### **Related Work and Connections**



I. Alice and Bob have access to trusted local sources of randomness.

- 2. Alice and Bob have access to an authenticated, but otherwise insecure classical channel.
- 3. No information leaves the laboratories unless the protocol allows it.
- 4. Alice and Bob have access to trusted classical operations
- 5. The devices do not have internal memories
- 6. The marginal states of Alice/Bob are independent whether Charlie's entangling measurement fails.

I. Alice and Bob have access to trusted local sources of randomness.

- 2. Alice and Bob have access to an authenticated, but otherwise insecure classical channel.
- 3. No information leaves the laboratories unless the protocol allows it.
- 4. Alice and Bob have access to trusted classical operations
- 5. The devices do not have internal memories
- 6. The marginal states of Alice/Bob are independent whether Charlie's entangling measurement fails.

### Assumptions I-4 are common assumptions

I. Alice and Bob have access to trusted local sources of randomness.

- 2. Alice and Bob have access to an authenticated, but otherwise insecure classical channel.
- 3. No information leaves the laboratories unless the protocol allows it.
- 4. Alice and Bob have access to trusted classical operations
- 5. The devices do not have internal memories
- 6. The marginal states of Alice/Bob are independent whether Charlie's entangling measurement fails.

### Assumptions I-4 are common assumptions

Current device-independent QKD uses assumptions 1-5

I. Alice and Bob have access to trusted local sources of randomness.

- 2. Alice and Bob have access to an authenticated, but otherwise insecure classical channel.
- 3. No information leaves the laboratories unless the protocol allows it.
- 4. Alice and Bob have access to trusted classical operations
- 5. The devices do not have internal memories
- 6. The marginal states of Alice/Bob are independent whether Charlie's entangling measurement fails.

Assumptions I-4 are common assumptions

Current device-independent QKD uses assumptions 1-5

Why do we need assumption 6?

• The marginal states of Alice/Bob are independent whether Charlie's entangling measurement fails.

• The marginal states of Alice/Bob are independent whether Charlie's entangling measurement fails.



• The marginal states of Alice/Bob are independent whether Charlie's entangling measurement fails.



#### With the above assumption:

- The secret key fraction is independent of the distance between Alice and Bob.
- The protocol is secure as long as we see some Bell violation.

• The marginal states of Alice/Bob are independent whether Charlie's entangling measurement fails.



#### With the above assumption:

- The secret key fraction is independent of the distance between Alice and Bob.
- The protocol is secure as long as we see some Bell violation.

## However, if the Bell violation is maximal, then the above assumption can removed!!

Note: we also have the security bound for non-maximal Bell violation with the assumption removed.



### Summary

#### At hand: A security proof that has the following features

- •Applies to a very general class of devices.
- •Only two parameters are required to bound the secrecy of the key.
- •Performs well in the finite key size regime.

### Summary

#### At hand: A security proof that has the following features

- •Applies to a very general class of devices.
- •Only two parameters are required to bound the secrecy of the key.
- •Performs well in the finite key size regime.

Interesting points:

- •Reaches the BB84 key rate (for qubits) in the limiting case.
- Local CHSH tests are independent of the distance between Alice and Bob (towards a loophole-free Bell test).

### Summary

#### At hand: A security proof that has the following features

- •Applies to a very general class of devices.
- •Only two parameters are required to bound the secrecy of the key.
- •Performs well in the finite key size regime.

Interesting •Reaches the BB84 key rate (for qubits) in the limiting case.

#### Local CHSH tests are independent of the distance between Alice and Bob (towards a loophole-free Bell test).

### In other words..

points:

It is "device-independent" and is secure against the most general attacks in the finite key size regime.

# Relevant Work in QCRYPT2012

### Talks

- Memory attacks on device-independent quantum cryptography
- A quantum key distribution system immune to detector attacks

### Poster

- Alternative schemes for measurement device independent QKD
- Device independent QKD with Reused Devices
- Security Proof of two-way QKD protocols with partial device independence
- Semi-device Independent QKD based on BB84 and a CHSH type estimation
- The link between entropic uncertainty and non-locality

# Relevant Work in QCRYPT2012

### Talks

- Memory attacks on device-independent quantum cryptography
- A quantum key distribution system immune to detector attacks

### Poster

- Alternative schemes for measurement device independent QKD
- Device independent QKD with Reused Devices
- Security Proof of two-way QKD protocols with partial device independence
- Semi-device Independent QKD based on BB84 and a CHSH type estimation
- The link between entropic uncertainty and non-locality

# Supplementary Information

For more details, please refer to arXiv:1208.0023